

Real-Time Control and Online Parameter Estimation for Drill String Dynamics Modeling

MATLAB Energy Conference 2021

Dr. Roman Shor
Associate Professor
Associate Head – Undergraduate Studies
Department of Chemical and Petroleum Engineering
University of Calgary, Calgary, Canada

November 16, 2021

Dr. Ulf Jakob Aarsnes
Research Scientist
NORCE

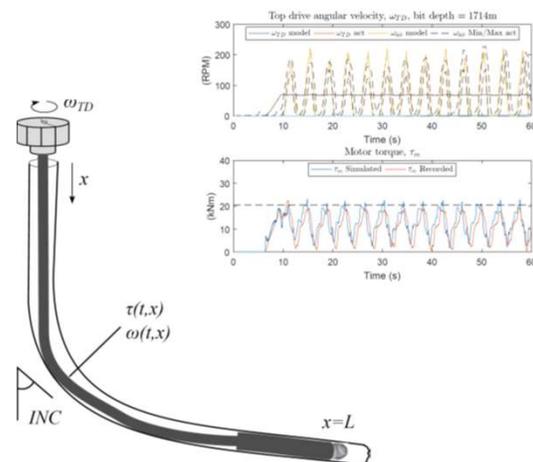
Dr. Florent Di Meglio
Professor
MINES ParisTech



1

Agenda

- Introduction & Motivation
- Drillstring & Friction Model
- Field Validation
- Stick-slip Mitigation Systems
- Benchmarking Systems
- Simulation Study
- Conclusions & Further Work



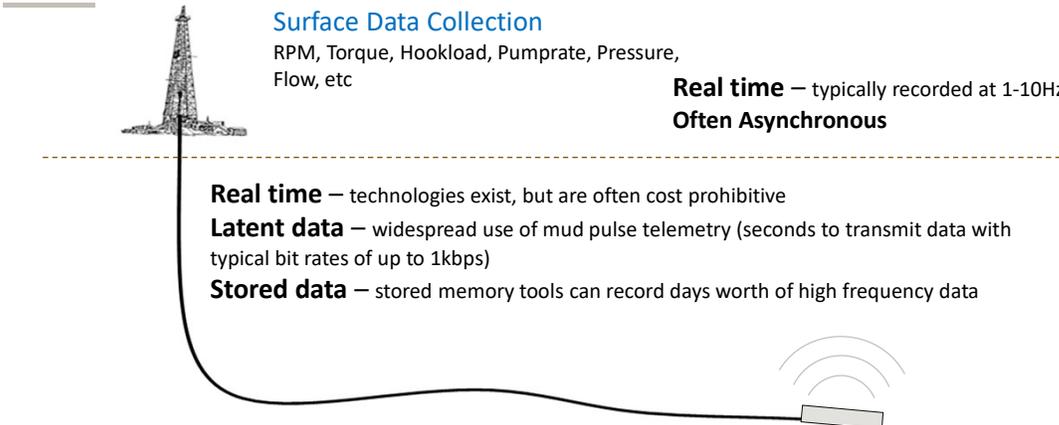
2

(c) Roman J. Shor | University of Calgary



2

Introduction



Surface Data Collection
RPM, Torque, Hookload, Pumprate, Pressure, Flow, etc

Real time – typically recorded at 1-10Hz
Often Asynchronous

Real time – technologies exist, but are often cost prohibitive

Latent data – widespread use of mud pulse telemetry (seconds to transmit data with typical bit rates of up to 1kbps)

Stored data – stored memory tools can record days worth of high frequency data

Downhole Data Collection
RPM, Torque, Weight-on-bit, Pressure, Vibration, etc

3

(c) Roman J. Shor | University of Calgary



3

Introduction



Copyright | reelwell

Source: bridgat.com

Source: everypart.com

Source: newoilrigs.com

Source: mudpumps.org

Source: eaglefordshale.com

Modified from reelwell

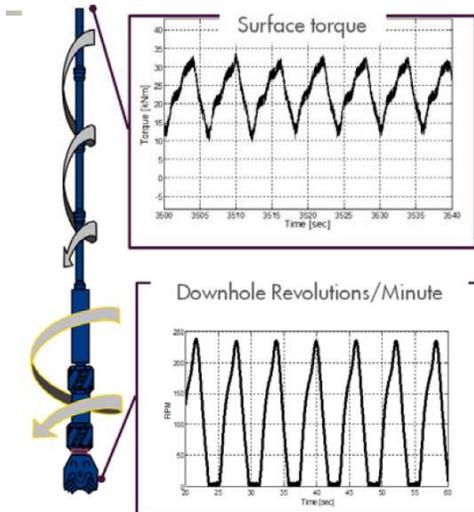
4

(c) Roman J. Shor | University of Calgary



4

What is Stick-Slip?



- Cyclic stopping (sticking) and releasing (slipping) of the bit and bottom hole assembly during drilling operations
- 3-10 second period (dependent on drillstring length)
- Visible at surface as a fluctuation in torque

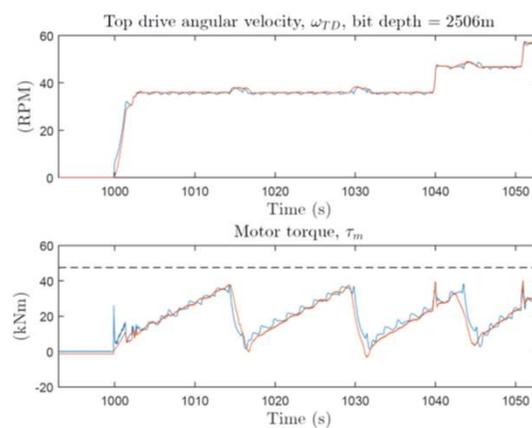
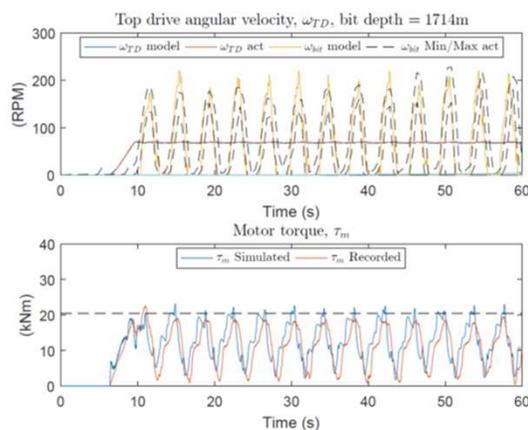
Runia et al., 2013
5

(c) Roman J. Shor | University of Calgary



5

Motivation

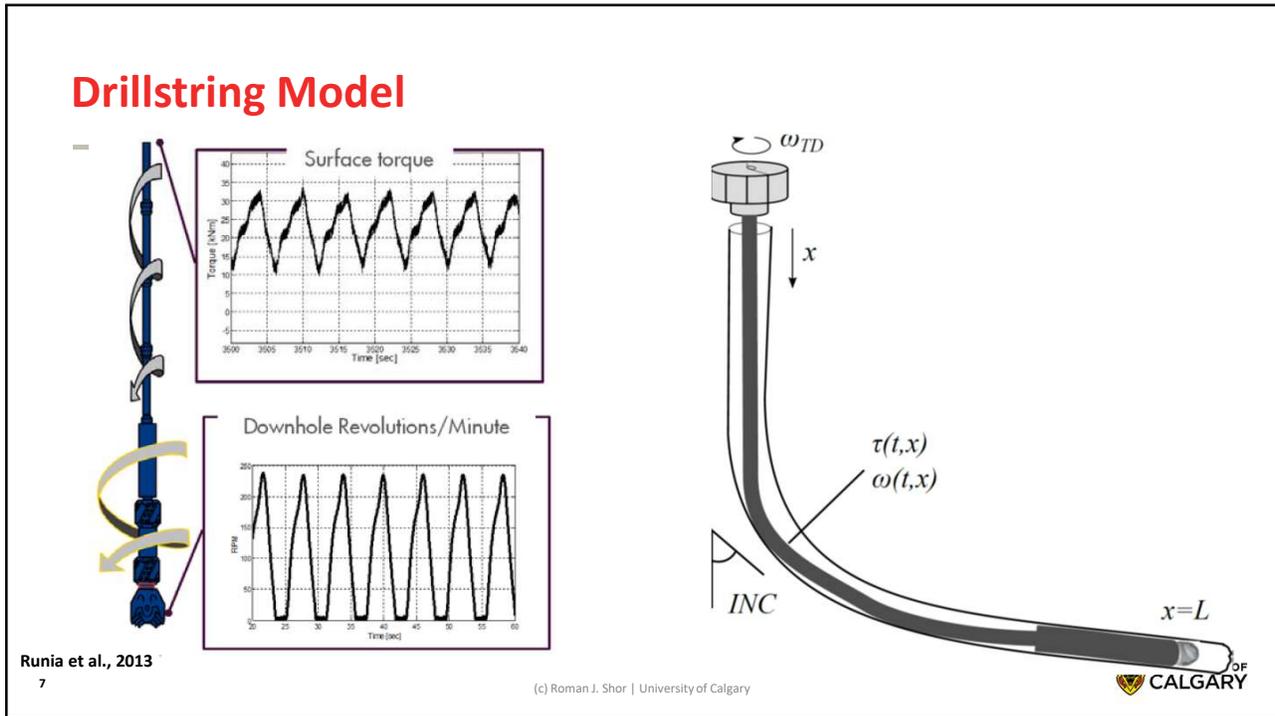


6

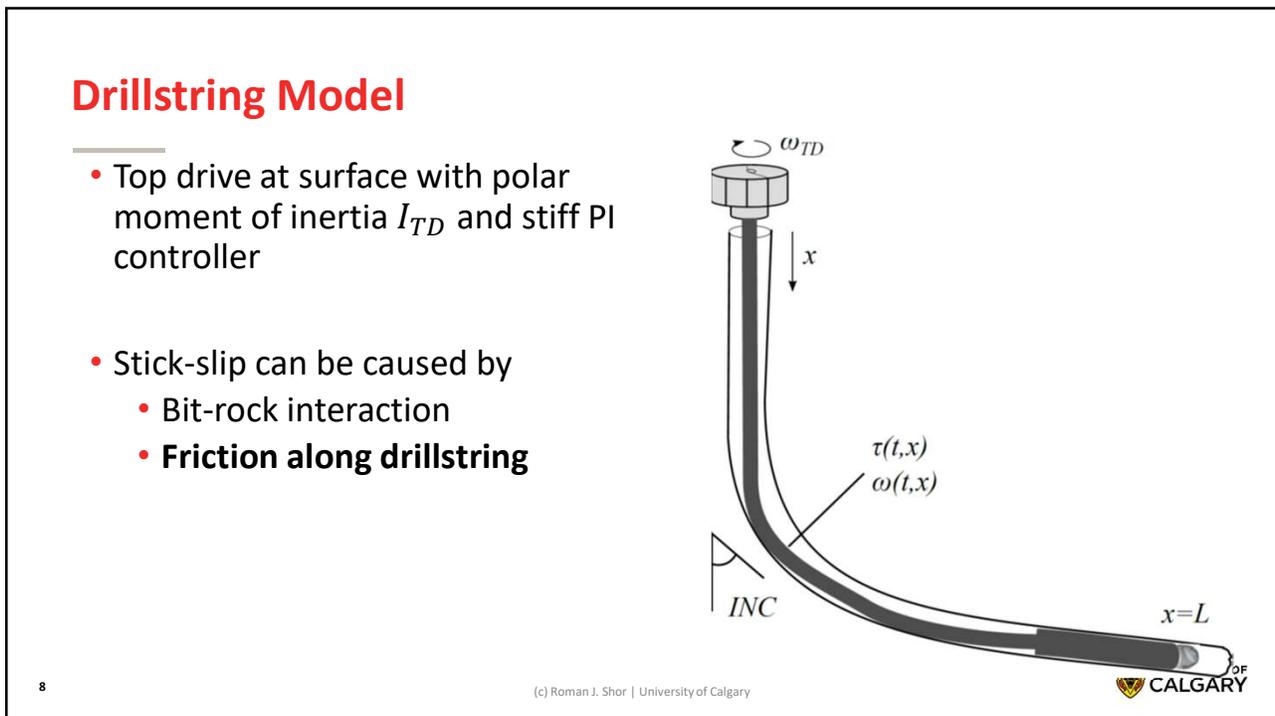
(c) Roman J. Shor | University of Calgary



6



7



8

Drillstring Model

9

(c) Roman J. Shor | University of Calgary

9

Drillstring Model

- Dynamics governed by the torsional wave equation

$$\frac{\partial \tau(t, x)}{\partial t} + JG \frac{\partial \omega(t, x)}{\partial x} = 0$$

$$J\rho \frac{\partial \omega(t, x)}{\partial t} + \frac{\partial \tau(t, x)}{\partial x} = S(\omega, x)$$
- where

τ – torque ω – angular velocity ρ – density	J – polar moment of inertia G – shear modulus
--	--

10

(c) Roman J. Shor | University of Calgary

10

Drillstring Model

- Dynamics governed by the torsional wave equation

$$\frac{\partial \tau(t, x)}{\partial t} + JG \frac{\partial \omega(t, x)}{\partial x} = 0$$

$$J\rho \frac{\partial \omega(t, x)}{\partial t} + \frac{\partial \tau(t, x)}{\partial x} = S(\omega, x)$$
- Source term is modeled by Coulomb Friction

$$S(\omega, x) = -k_t \rho J \omega(t, x) - \mathcal{F}(\omega, x)$$

11
(c) Roman J. Shor | University of Calgary

11

Coulomb Friction

- Coulomb friction is modeled as an inclusion

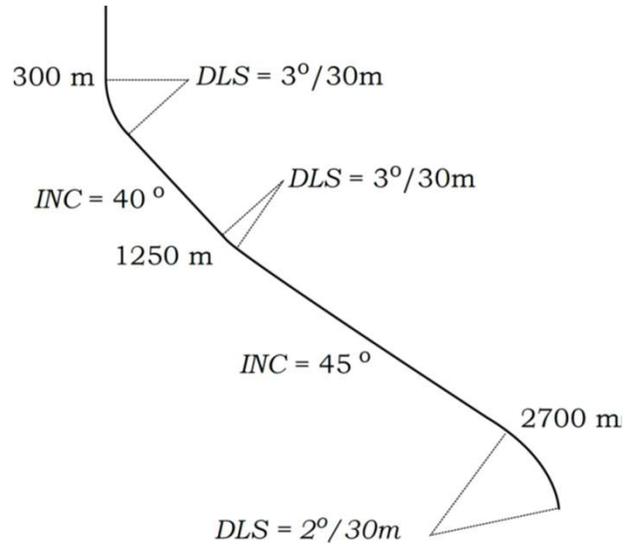
$$\begin{cases} \mathcal{F}(\omega, x) = F_d(x), & \omega > \omega_c, \\ \mathcal{F}(\omega, x) \in [-F_c(x), F_c(x)], & |\omega| < \omega_c, \\ \mathcal{F}(\omega, x) = -F_d(x), & \omega < -\omega_c, \end{cases}$$
- with the parameters:
 - F_c , maximum Coulomb torque, or alternatively, μ , coefficient of friction
 - ω_c , the transition angular velocity
 - k_t , the viscous friction coefficient

12
(c) Roman J. Shor | University of Calgary

12

Field Example

- Inertia dominated oscillations
- 200 Hz surface data
- 10s min/max/mean downhole data



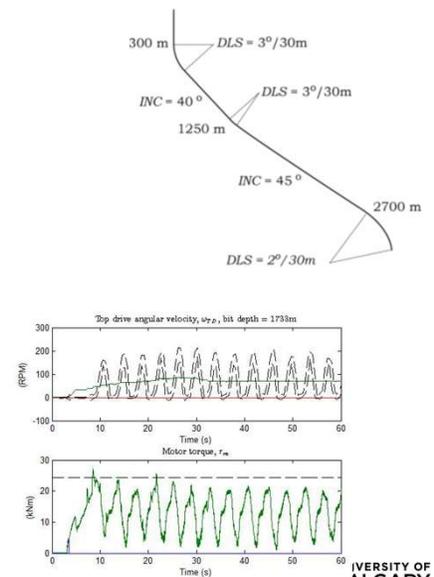
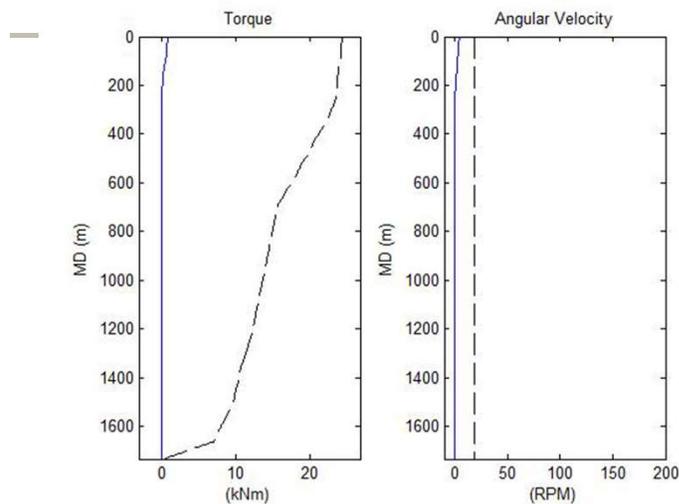
13

(c) Roman J. Shor | University of Calgary



13

Field Example

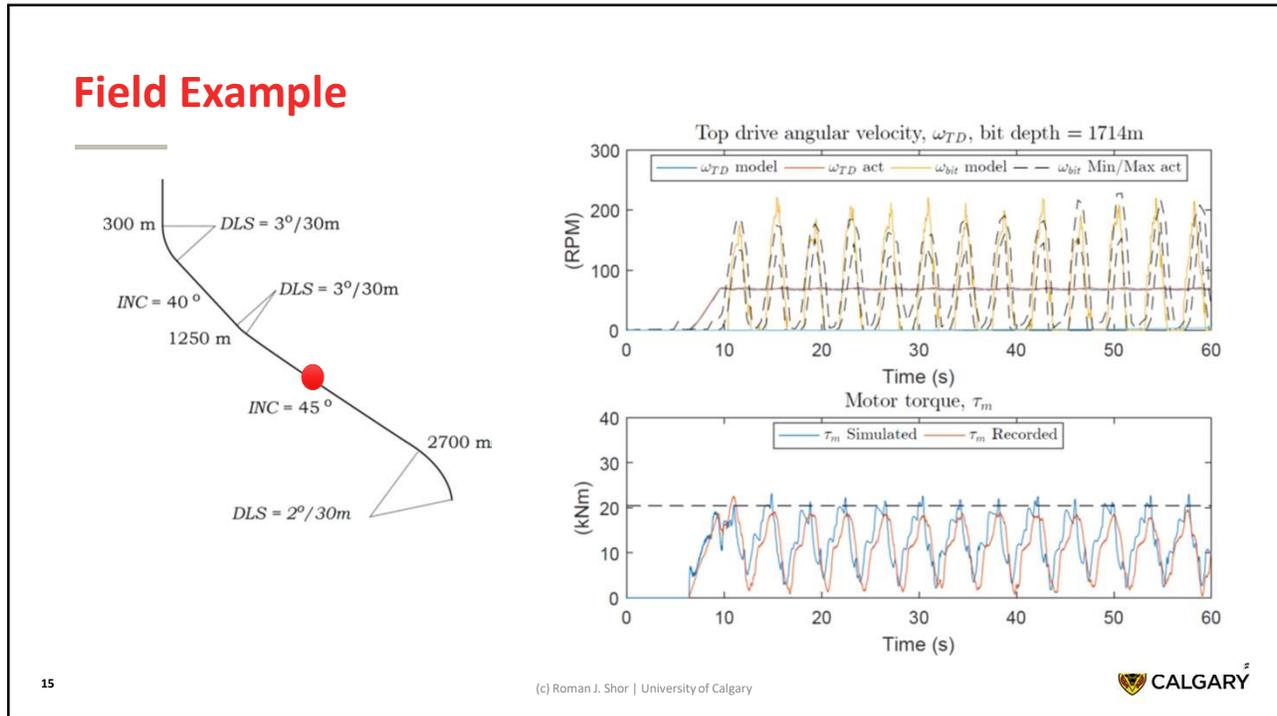


14

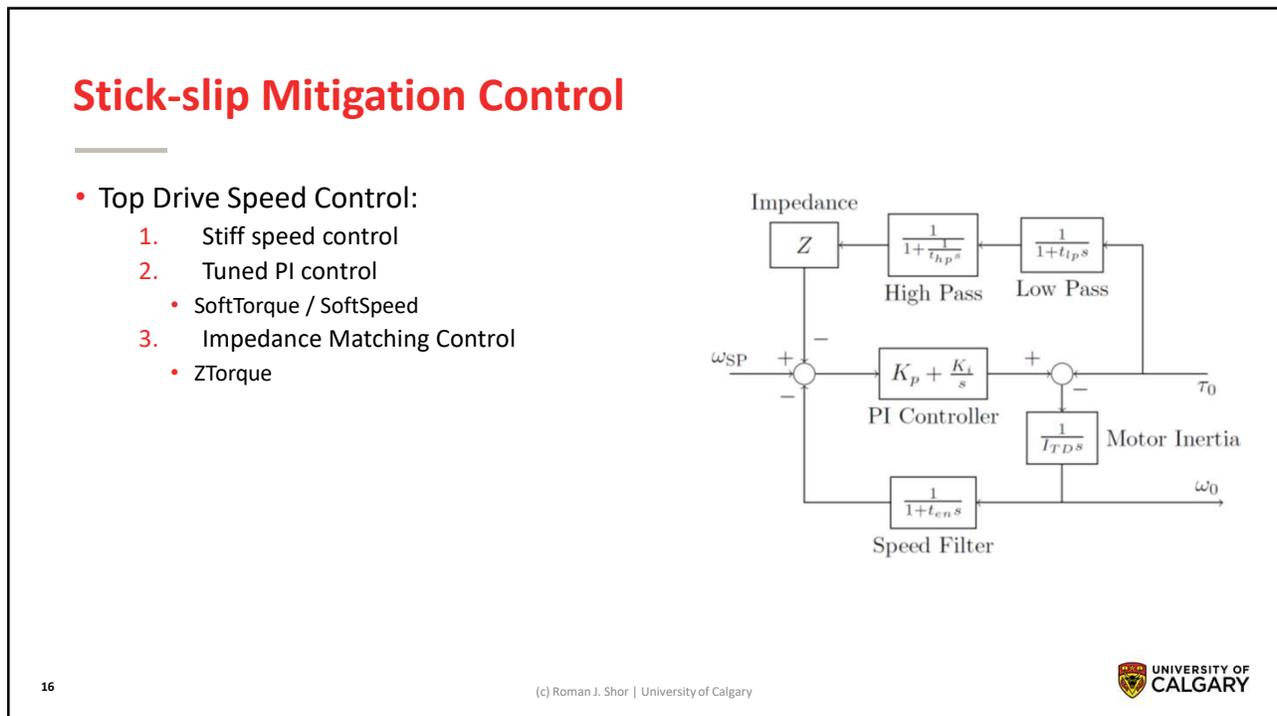
(c) Roman J. Shor | University of Calgary



14



15



16

Stick-slip Mitigation Control

- Top Drive Speed Control:

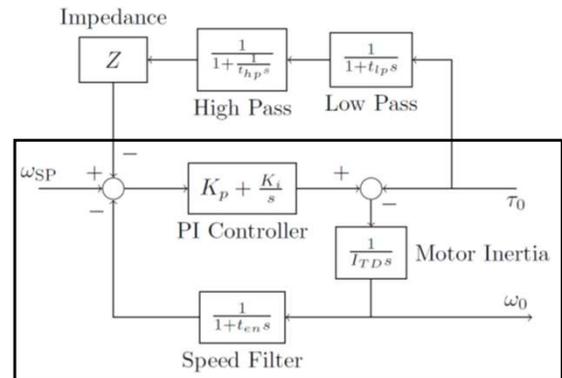
- **Stiff speed control**

- $K_p = 100\zeta_p$

- $K_i = 5I_{TD}$

- where,

$\zeta_p = J_p \sqrt{G_p \rho}$ is pipe impedance, and I_{TD} is the top drive inertia



17

(c) Roman J. Shor | University of Calgary



17

Stick-slip Mitigation Control

- Top Drive Speed Control:

- **Tuned PI control**

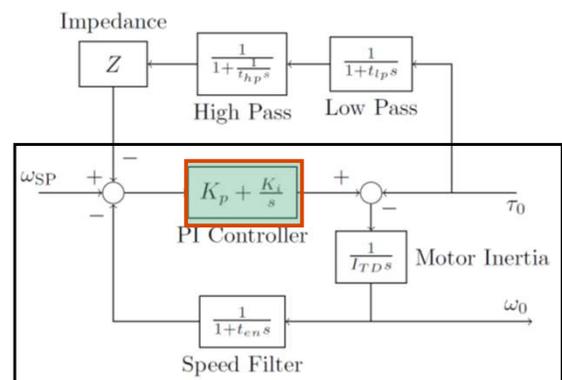
- Marketed as SoftTorque / SoftSpeed

- $K_p = 4\zeta_p$

- $K_i = (2\pi f_c)^2 I_{TD}^2$

- where,

f_c is the frequency (in Hz) of minimal reflectivity



18

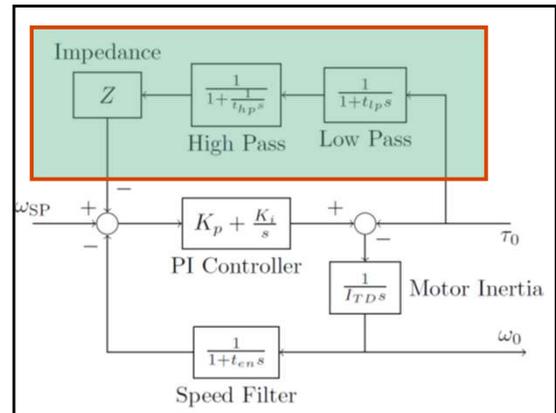
(c) Roman J. Shor | University of Calgary



18

Stick-slip Mitigation Control

- Top Drive Speed Control:
 - **Impedance Matching Control**
 - Marketed as Ztorque
 - Desired top drive speed to match pipe impedance given by
 - $\omega_o(t) = \frac{1}{\zeta_p} \cdot \tau_o(t)$



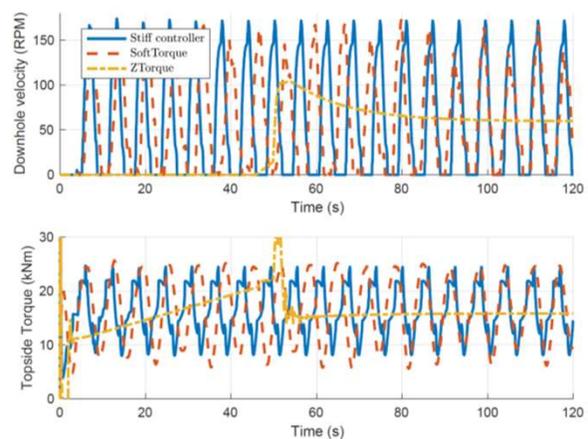
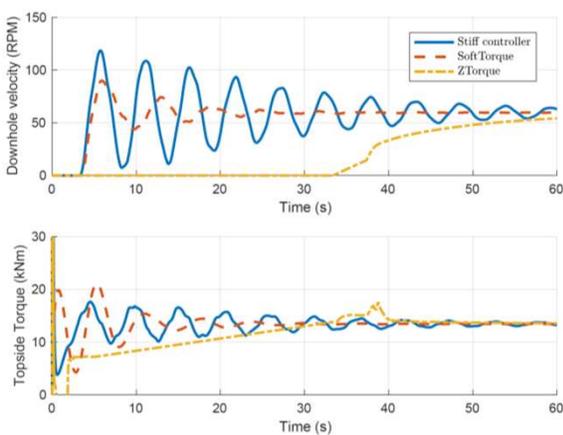
19

(c) Roman J. Shor | University of Calgary



19

Stick-slip Mitigation Control



20

(c) Roman J. Shor | University of Calgary



20

Evaluating Performance

- Concept of *reflectivity*

$$R(\omega) = \left| \frac{\bar{C}(s) - \zeta_p}{\bar{C}(s) + \zeta_p} \right|$$

where

$$\bar{C}(s) = \frac{\tau_o(s)}{\omega_o(s)} = C(s) + I_{td}s = \frac{\tau_m(s)}{\omega_o(s)} + I_{td}s$$
$$\zeta_p = J_p \sqrt{G_p \rho}$$

21

(c) Roman J. Shor | University of Calgary



21

Top Drive Reflectivity

- **Traditional stiff speed controller**
 - Reflects torsional waves back to the bit



22 22

(c) Roman J. Shor | University of Calgary



22

Top Drive Reflectivity

- **Traditional stiff speed controller**
 - Reflects torsional waves back to the bit

- **Ideal zero reflection boundary**
 - Transmits all wave energy into space and does not reflect it downhole



23 23

(c) Roman J. Shor | University of Calgary



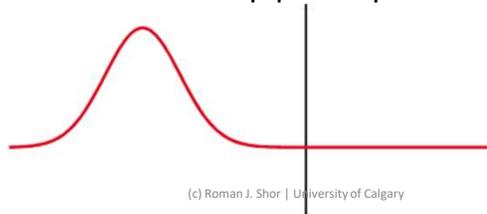
23

Impedance Matching Control

- **Impedance Matching**
 - The drillstring has a **characteristic impedance**, which can be calculated

$$\zeta_p = J_p \sqrt{\rho G} = \frac{\omega_0}{\tau_0}$$

- A control system may then **match** the drillpipe impedance by changing rpm based on sensed pipe torque



24

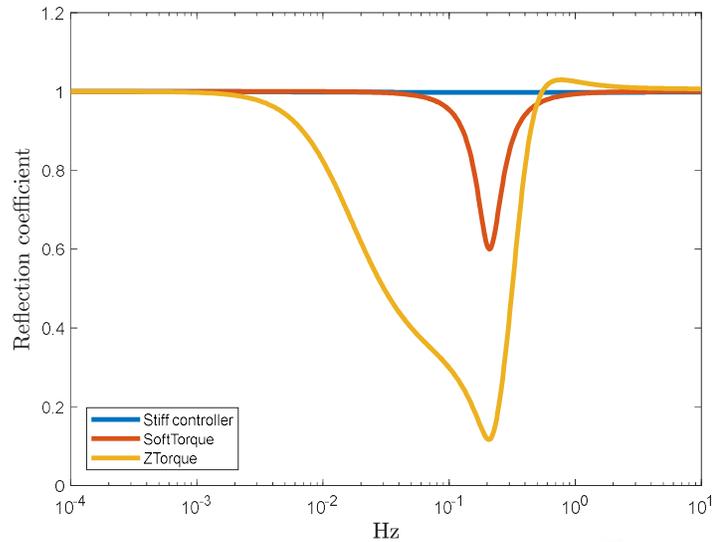
(c) Roman J. Shor | University of Calgary



24

Evaluating Effectivity

- **Stiff speed:** reflectivity of 1 at all frequencies
- **SoftTorque:** reflectivity reduced at tuning frequency
- **Ztorque:** improved range of reduced reflectivity.
 - Limited by:
 - Tracking performance (high pass filter).
 - Instrumentation constraints (low pass filters and delays).



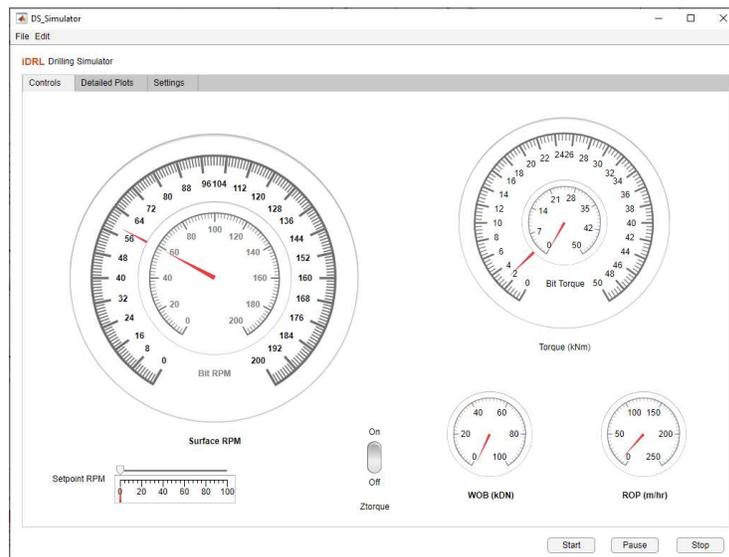
25

(c) Roman J. Shor | University of Calgary



25

Data Evaluation



26

(c) Roman J. Shor | University of Calgary



26

Data Evaluation

27

(c) Roman J. Shor | University of Calgary



27

Conclusions

- Basic torsional model able to replicate different modes of stick slip caused by side forces
 - Ratio between static and kinematic friction key parameter
- Industry controllers tested using model:
 - SoftTorque/SoftSpeed reduces stick-slip tendency but may increase severity when the ratio between static and kinematic friction is below 0.8
 - Ztorque with torque measurement removes stick slip
(but might be limited by delays / latency / filtering in practice)
- Reflectivity coefficient good predictor of performance.

28

(c) Roman J. Shor | University of Calgary



28

Acknowledgements

- Sicco Dwars at **Shell International Exploration and Production**
- Eric Cayeux at **NORCE**

- Research Council of Norway, ConocoPhillips, Det norske oljeselskap, Lundin, Statoil and Wintershall through the research center **Drill-Well** (203525/O30) at **NORCE**

- Schulich School of Engineering at the **University of Calgary**