

MathWorks
**AUTOMOTIVE
CONFERENCE 2023**
Korea

The development status of HMC vehicle dynamics model using MATLAB/Simulink

Lee, Jinhwa, Hyundai Motor Group

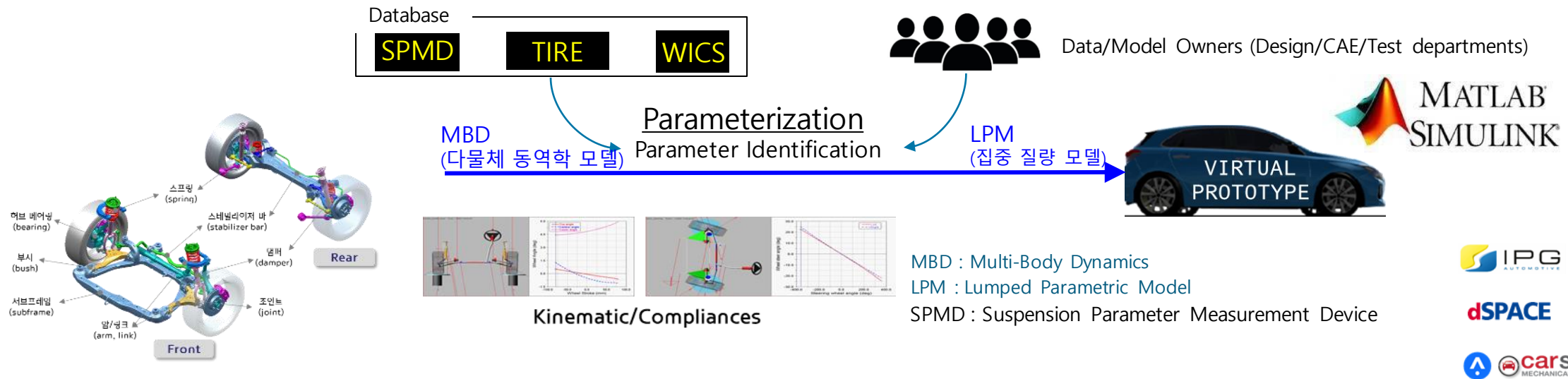
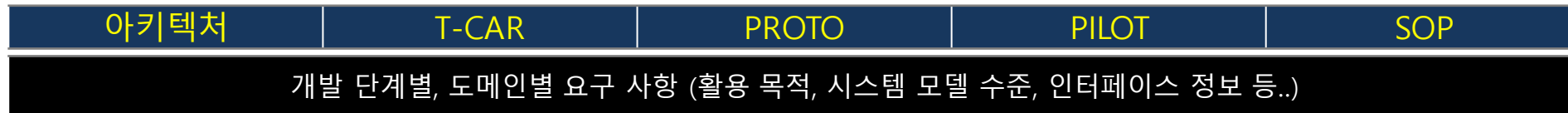


Contents

- Introduction
- The Model and its understanding
- Environment of Model Development
- Model V&V Process
- Summary

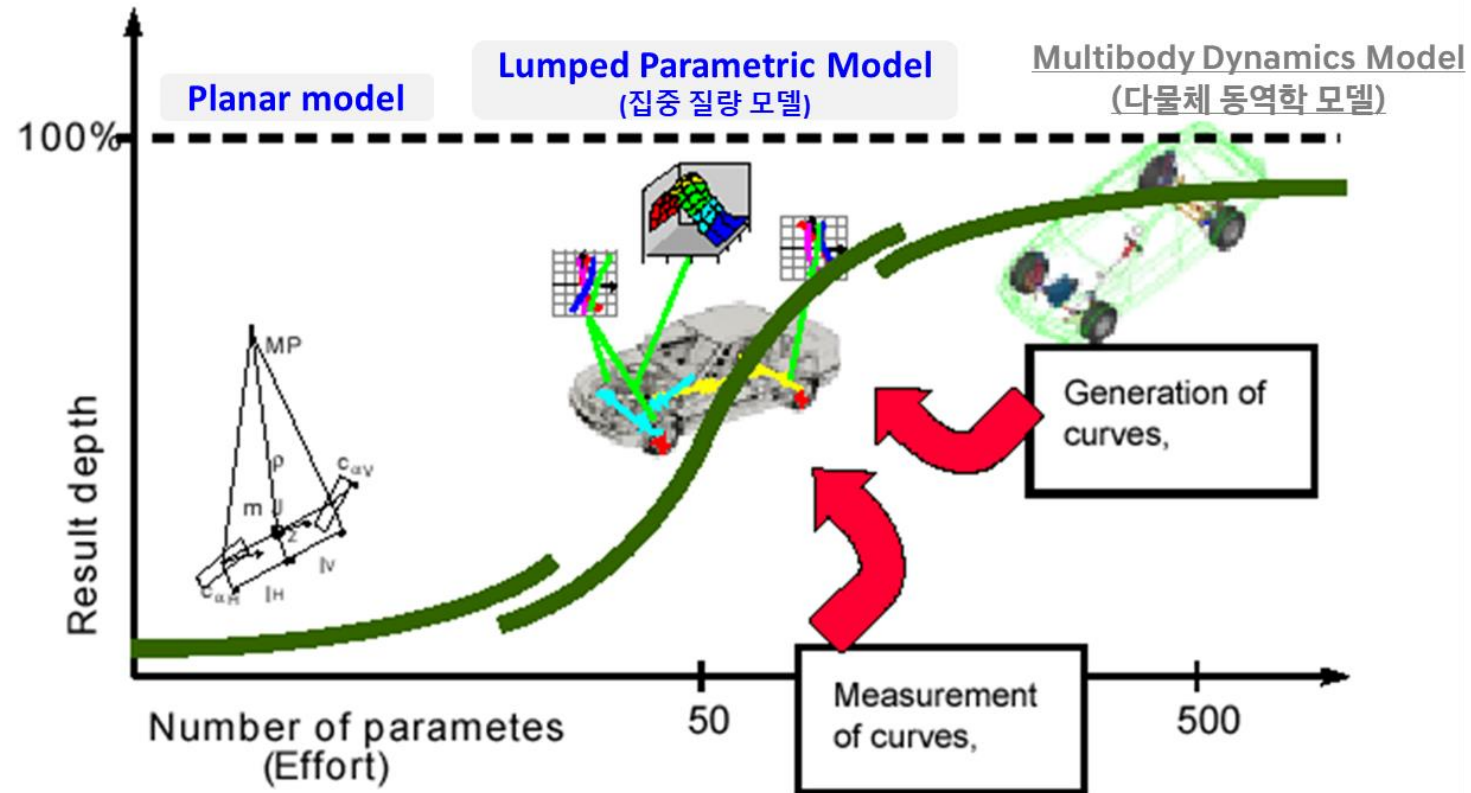
Introduction

Vehicle model development and distribution
for System/SW verification/validation(V&V)/performance development



The Model and Its Understanding

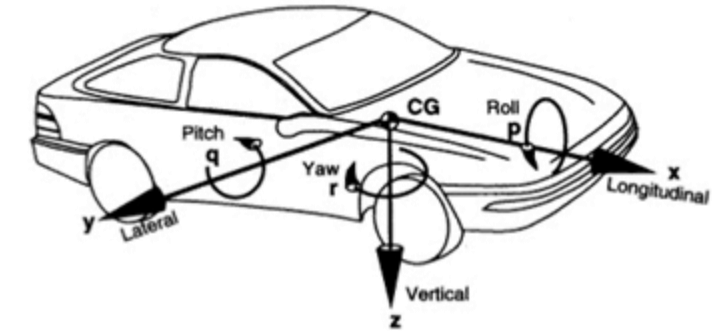
Reduced Order Model based on CAE Model and Test Measurement

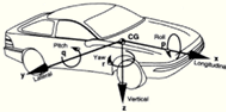
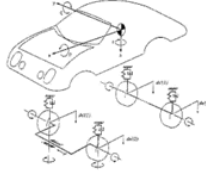
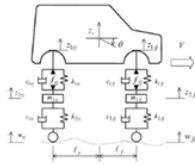
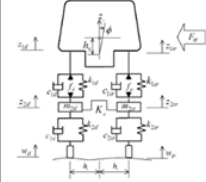
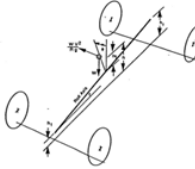
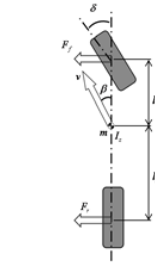
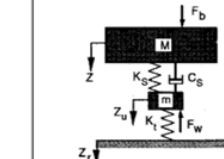
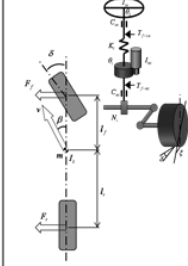


“ADAMS/Car-AT in The Chassis Development at BMW” Ewald Fischer, BMW, 14. November 2001

The Model and Its Understanding

① Planar Models using MATLAB/Simulink

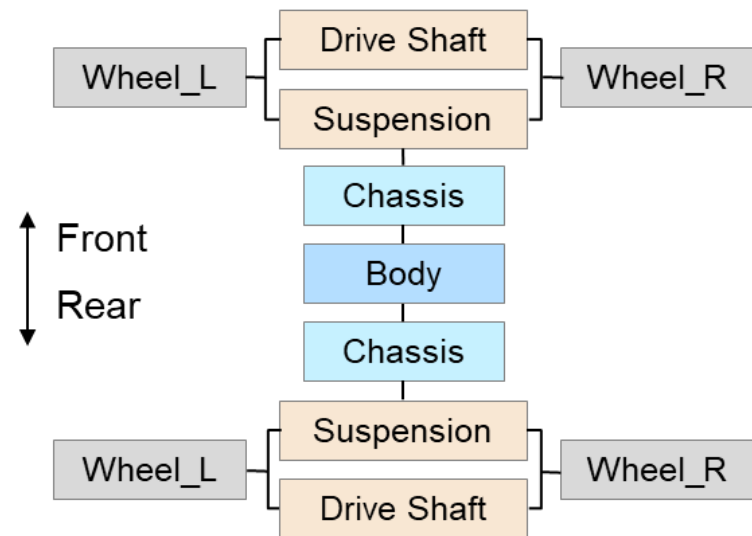


분류		Full vehicle	피치 모델	롤 모델	횡+요+롤	Bicycle	Quarter car	Steering
								
차량 거동	횡방향	●		●	●	●		●
	수직방향	●	●	●	●		●	
	스티어링							●
	종방향	●						
운동 자유도 (d.o.f)	Sprung	6	2	2	3	2	1	2
	Unsprung	4	2	2	-	-	1	-
	Wheel	4	-	-	-	-	-	-
	Steering	-	-	-	-	-	-	2
	Total	14	4	4	3	2	2	4

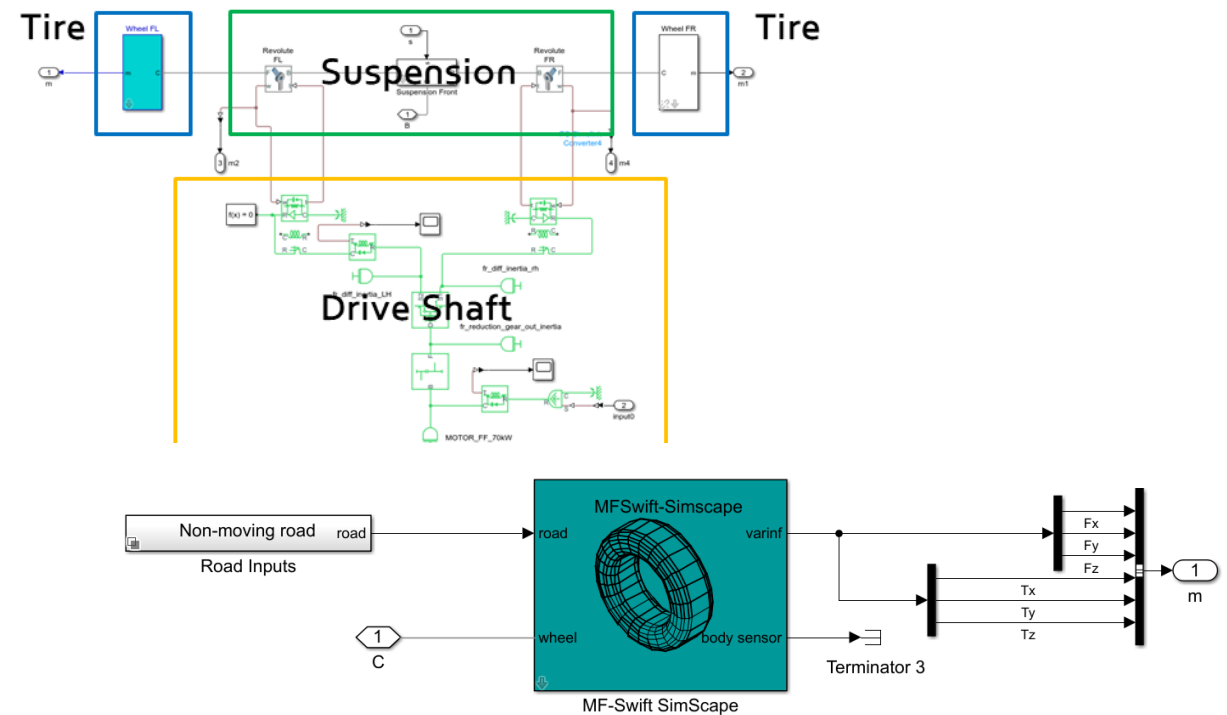
The Model and Its Understanding

For example, 14DOF vehicle dynamics model + MF-SWIFT using **Simscape**

Vehicle Body(6DOF) + Wheel vertical (4DOF) + Wheel spin (4DOF)



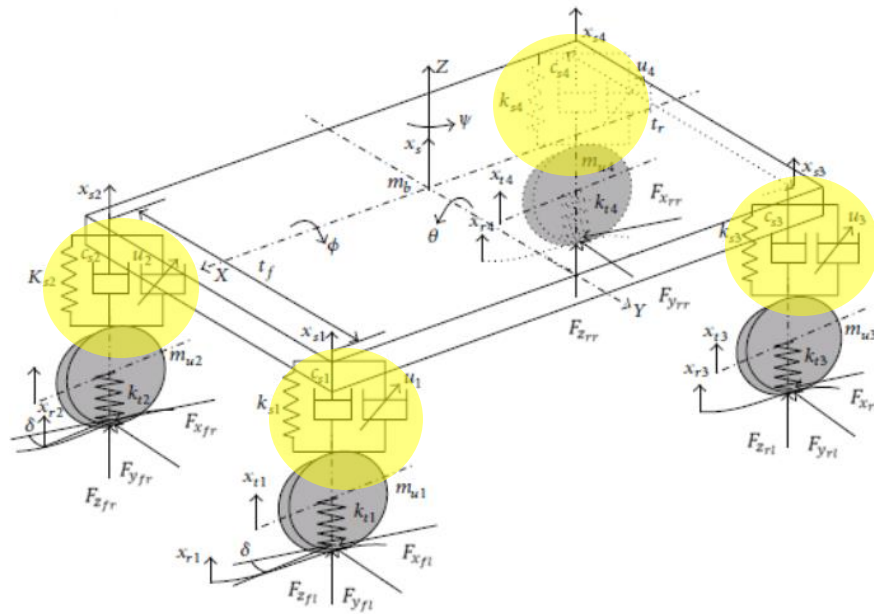
[Chassis Simulink Model Structure]



The Model and Its Understanding

② Lumped Parametric Model

A vehicle model that configures the Kinematic/Compliance characteristics of a suspension system in the form of a function through wheel relative motion (displacement, speed, acceleration) equation for a vehicle body based on 17 DOF model



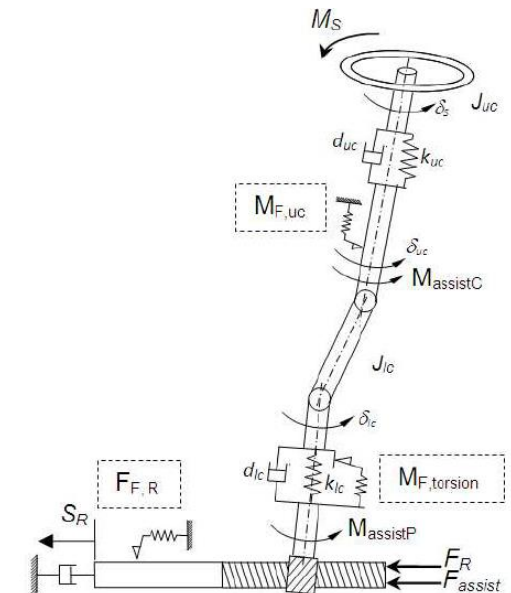
Vehicle Body 6DOF + (Wheel Vertical 1DOF + Wheel Rotation 1DOF) x 4 = 14 DOF

$$y'_{w/b} = f(\delta_r, \delta_l) + s'_w$$

$$y_w = y_b + A_b y'_{w/b}$$

$$\dot{y}' = \begin{bmatrix} \dot{y}'_b \\ \dot{y}'_w \end{bmatrix} = B \begin{bmatrix} \dot{\delta}_r \\ \dot{\delta}_l \end{bmatrix} = B$$

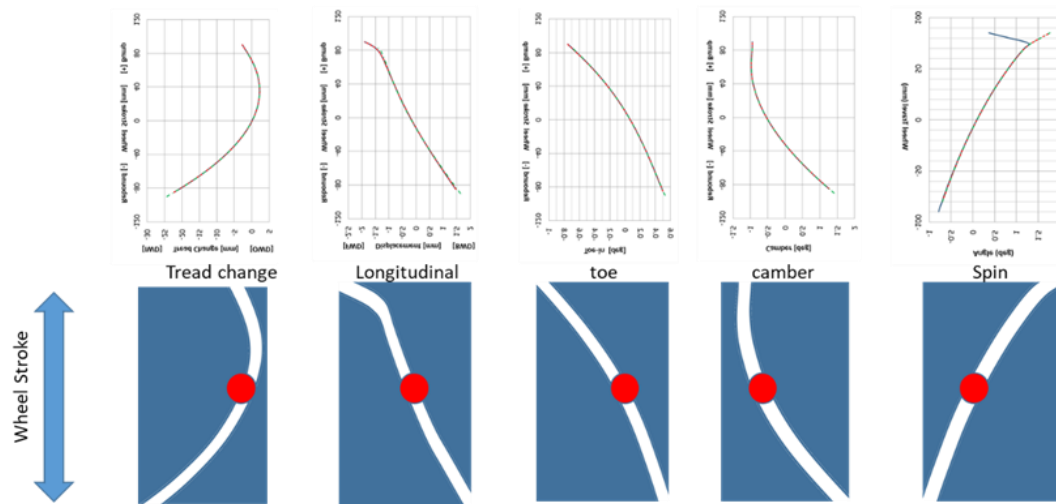
$$\ddot{y}' = \begin{bmatrix} \ddot{y}'_b \\ \ddot{y}'_w \end{bmatrix} = \dot{B} \begin{bmatrix} \dot{\delta}_r \\ \dot{\delta}_l \end{bmatrix} + B \begin{bmatrix} \ddot{\delta}_r \\ \ddot{\delta}_l \end{bmatrix}$$



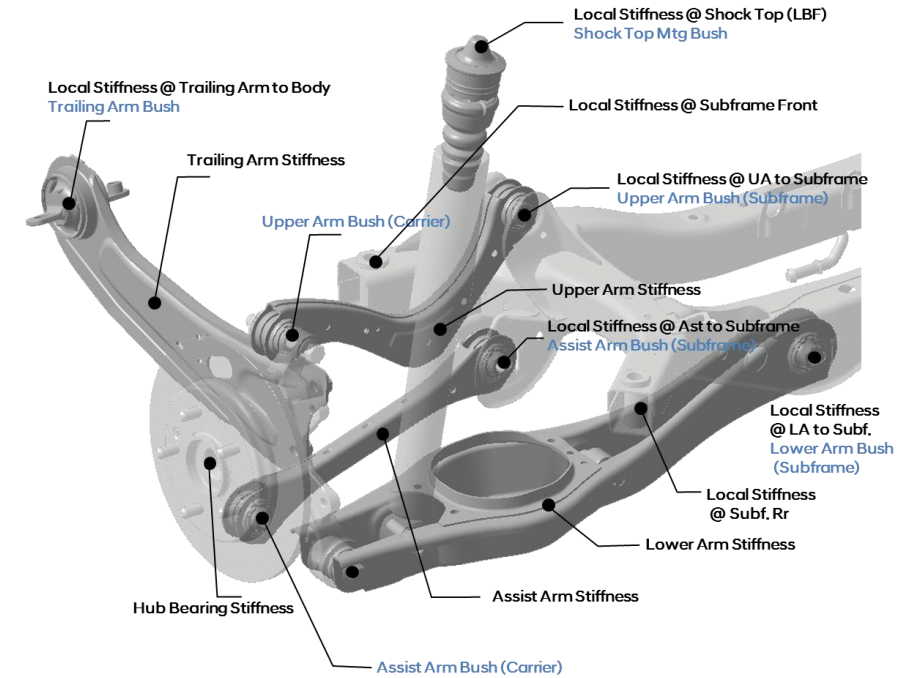
Steering system 3DOF

The Model and Its Understanding

Kinematic/Compliance Modeling from MBD simulations



2 Translations + 3 rotations : 5 variables need to be defined
 Polynomial / Lookup table
 (wheelbase, tread, toe, camber, caster by wheel stroke/rack stroke)



$$c = \frac{\partial q}{\partial Q} =$$

2.70E-06	-3.46E-11	-1.69E-10	-5.30E-06	-1.19E-09	-4.15E-10	2.03E-07	2.80E-07	1.25E-09	1.03E-06
-4.37E-11	1.18E-07	-7.20E-08	1.13E-10	-3.75E-07	2.02E-07	-6.15E-12	5.91E-12	-2.76E-07	-1.75E-11
-1.80E-10	-7.20E-08	1.91E-06	-1.66E-10	1.14E-06	3.09E-07	9.01E-13	9.49E-11	-7.73E-07	1.28E-09
-5.30E-06	9.24E-11	-1.87E-10	2.04E-05	-3.11E-09	1.22E-09	-3.98E-07	-2.93E-07	-1.27E-09	-3.74E-06
-1.13E-09	-3.74E-07	1.13E-06	-3.23E-09	8.41E-06	4.61E-07	-1.09E-11	1.31E-09	-4.14E-06	1.44E-08
-4.14E-10	2.02E-07	3.10E-07	1.24E-09	4.65E-07	2.70E-06	-3.34E-11	-1.67E-10	-5.04E-06	-1.19E-09
2.03E-07	-6.20E-12	-9.16E-13	-3.99E-07	-1.92E-11	-4.25E-11	8.79E-08	-2.09E-07	1.04E-10	-3.25E-07
2.79E-07	7.38E-12	9.64E-11	-2.90E-07	1.30E-09	-1.79E-10	-2.09E-07	1.95E-06	-1.91E-10	1.00E-06
1.22E-09	-2.76E-07	-7.75E-07	-1.27E-09	-4.15E-06	-5.04E-06	8.29E-11	-2.16E-10	1.89E-05	-3.14E-09
1.03E-06	-1.01E-11	1.30E-09	-3.74E-06	1.43E-08	-1.13E-09	-3.24E-07	9.94E-07	-3.25E-09	4.77E-06

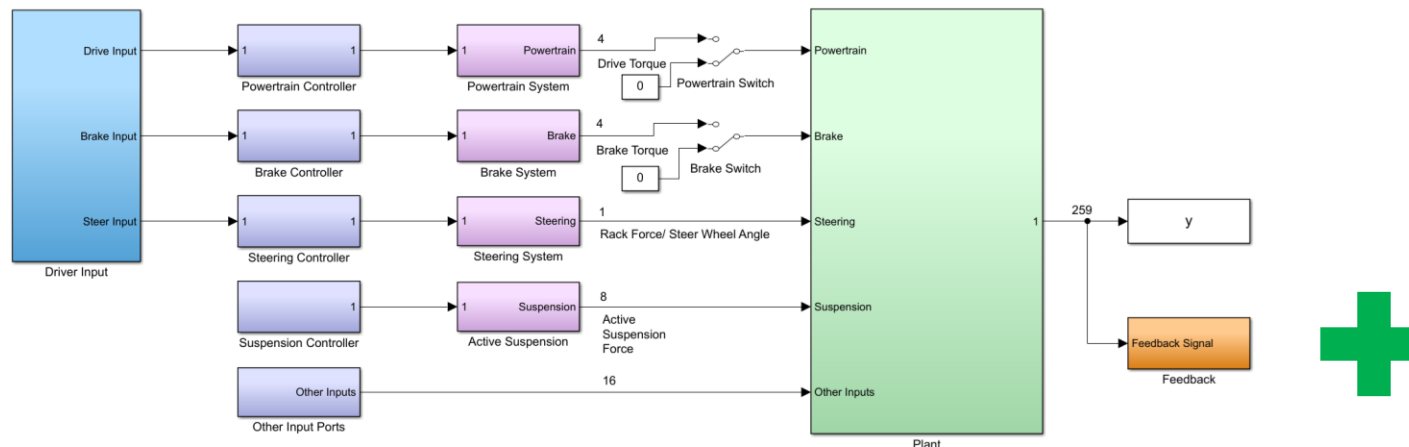
Compliance Matrices

The Model and Its Understanding

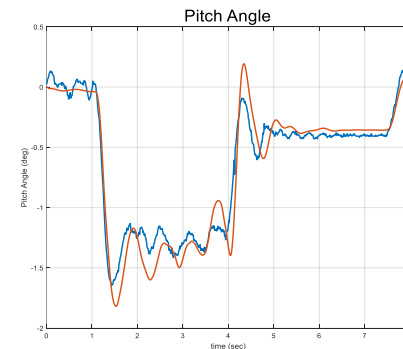
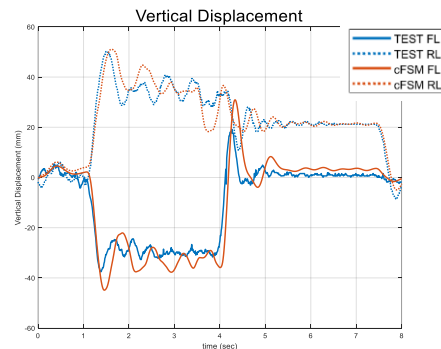
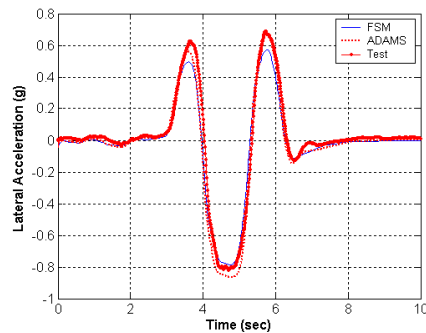
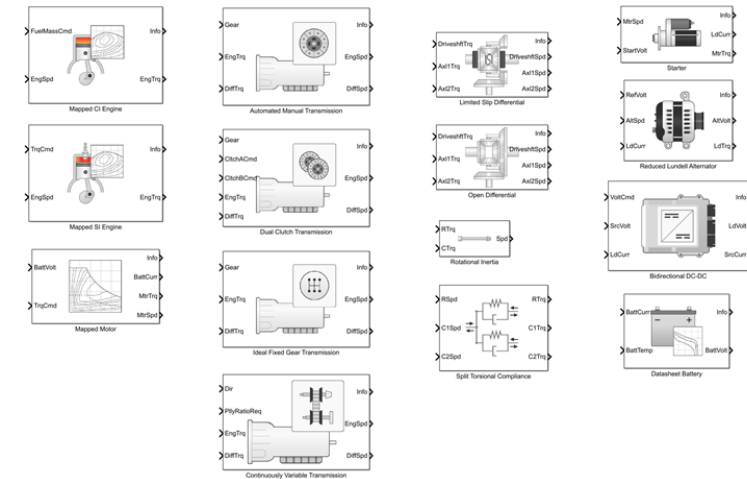
Simulink based Vehicle Dynamics Model by VDL (On-going) VDL(주브이디엘) from Kookmin Univ. Vehicle Dynamics Lab.

Development of a vehicle model suitable for SW Virtual Testing using **Powertrain Blockset** in Simulink and developed vehicle dynamics model for around 10 years with HMC

Vehicle Dynamics Model w/o Powertrain system



Powertrain Blockset



← Validation with HMC chassis test teams

The Model and Its Understanding

Simulink based Vehicle Dynamics Model

This is why...

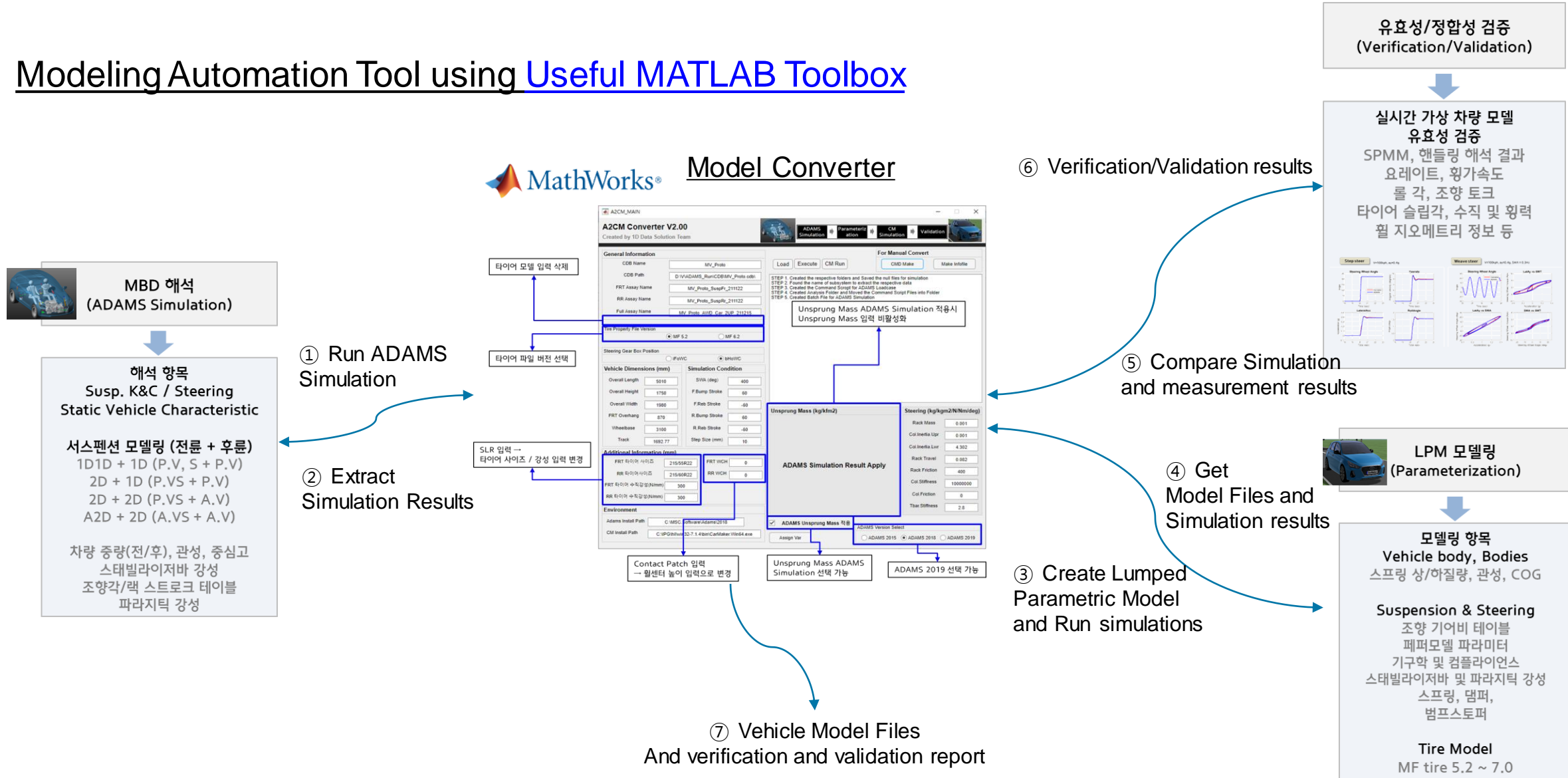
- MBD method is strongly required by SDV (Software Defined Vehicle) development strategy
- The Capabilities for integration and simulation of various controllers and development platform

Benefits

- Integration of various controllers using Native Simulink and Legacy Code and FMI
- Open environment that can be used as a common development tool for model readability and collaboration
- Applicable to optimization and controller development in connection with useful MATLAB/Simulink Toolbox
- Continuous use from MIL to HIL level through code generation support

Environment of Model Development

Modeling Automation Tool using Useful MATLAB Toolbox



Environment of Model Development

Tire Modeling, generally..

Test based method
: HMC, Tire Suppliers

FEM Based (just started..)
: Tire Suppliers

Test based

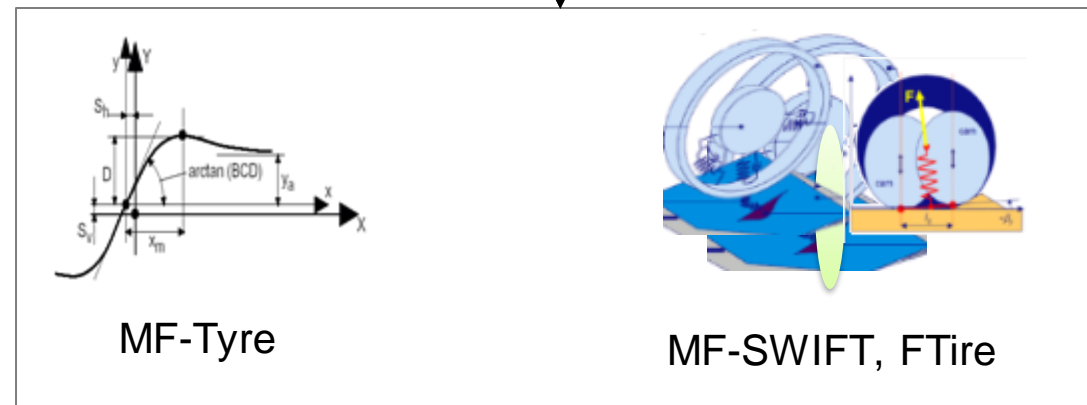
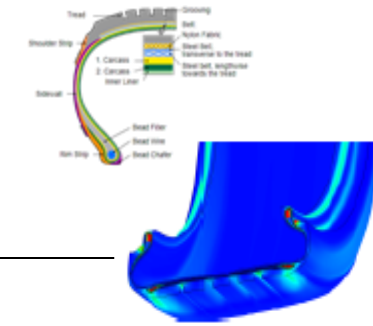


정특성

핸들링

동특성

FEM Based



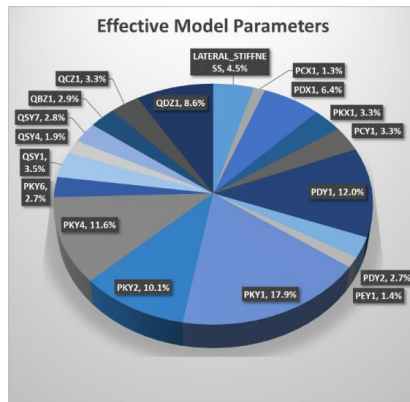
MF-Tyre

MF-SWIFT, FTire

Environment of Model Development

Tire Modeling, In case we cannot acquire tire model from previous method..

We are using design specifications/performance based tire modeling method using **MATLAB Optimization Toolbox / Python(GPR ML)**

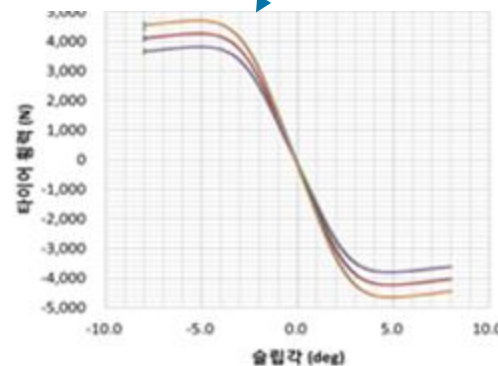


> Descriptions are available for the three steady-state modes of slip
 > Equations depend on vertical load F_z , inclination angle γ and inflation pressure p_i ; $[F_x, F_y, M_x, M_y, M_z] = MF(F_z, \kappa, \alpha, \gamma, p_i)$

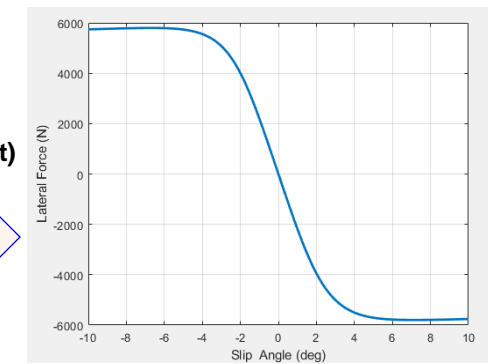
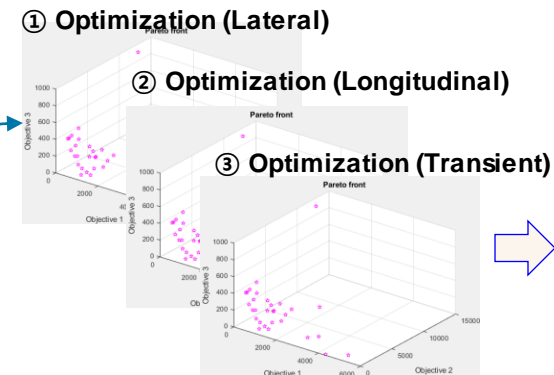
```

+ combinations
turn
+ Ca
- Output = [Ca Max_Fy Steady_Fy RelatL];
    
```

MATLAB script based MF tire modeling



Comparison with commercial Tire solver (dll)



Tire model parameter extraction to achieve functional tire characteristics using MATLAB Multi-objective genetic algorithm

Environment of Model Development

Its Front-end using App designer

Module 1
(7 design variables)

Input : 타이어 설계 변수

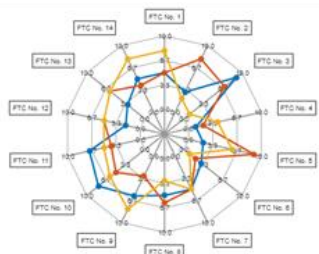
```
TDPs_struct_1 = struct(...
    "Mold_Tread_Depth", 7.0, ...
    "Belt_Angle", 24.0, ...
    "Cap_Ply_Material", 0.815, ...
    "Beadfiller_Height", 35.0, ...
    "Vertical_Load", 760.5, ...
    "Tread_Hardness", 0.8688, ...
    "Belt_Material", 1.0 ...
);
```

Module 3

Direct FTC input

* Functional Tire Characteristics

Spider chart



Functional Tire Characteristic Predictor

Tire Design Parameters

Tire Dimension and Test Condition
 NSW(mm) 265 Aspect Ratio(%) 45 Rim Dia (in) 19 Rim Width(J) 6.0 Inflation(psi) 34 Load(kg) 0

Tire Profile
 OD(mm) 771 SW(mm) 280 Tread Radius(mm) 960/590/260 Mold Depth(mm) 5 Tread Width(mm) 228

Sidewall and Tread Geometry
 Up SW Ga(mm) 3.5 Lo SW Ga(mm) 6.0

Tread Geometry and Property
 Hardness(HS) 55 Under gauge(mm) 1.7 Sub gauge(mm) 1

Belt Geometry and Property
 Width(mm) 230 Angle (deg) 21 Material 1+2(0.3) 19EPI

Carcass Geometry and Material
 TU Height(mm) 56 Cap ply mat Aramid Hybrid Cap ply type JFS

Bead Geometry and Property
 Height (mm) 20 Hardness 60

Predict Clear

Module 2

Input : 타이어 설계 변수

```
TDPs_struct_2 = struct(...
    "NSW", 275.0, ...
    "Series", 55.0, ...
    "Rim_Diameter", 20.0, ...
    "Inflation_Pressure", 36.0, ...
    "Rim_Width", 8.5, ...
    "Mold_Tread_Depth", 7.0, ...
    "Under_Tread_Gauge", 2.2, ...
    "Sub_Tread_Gauge", 1.5, ...
    "Belt_Width", 240.0, ...
    "Belt_Angle", 24.0, ...
    "Carcass_Material", 1.0, ...
    "Carcass1_Turn_Up_Height", 76.0, ...
    "Cap_Ply_Material", 0.815, ...
    "Cap_Ply_Type_Edge_Factor", 2.0, ...
    "Cap_Ply_Type_Center_Factor", 1.0, ...
    "Beadfiller_Height", 35.0, ...
    "Upper_Sidewall_Rubber_gauge", 4.5, ...
    "Lower_Sidewall_Rubber_Gauge", 8.5, ...
    "Tread_Width", 240.0, ...
    "Tread_Radius_1", 1200.0, ...
    "Tread_Radius_2", 590.0, ...
    "Tread_Radius_3", 190.0, ...
    "Mold_OD", 807.0, ...
    "Mold_SW", 290.0, ...
    "Vertical_Load", 760.5, ...
    "Tread_Hardness", 0.86884, ...
    "Belt_Material", 1.0, ...
    "Sho_Drop", 10.81, ...
    "Drop_At_TW85", 0.79 ...
);
```

To configure MF 5.2/6.2

Key Functional Tire Characteristics Details MF Tire Modeling F Tire Modeling

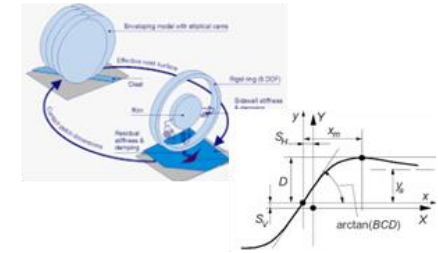
Predicted Characteristics

	FTC Values	Difference
Rolling Resistance Coeff	0.0244	0.1615
Cornering Stiff (N/deg)	0.9827	0.1788
Max.Lateral Frc	0.7302	0.4229
Relaxation Length(m)	0.3439	0.0942
G-function	0.5841	0.5955
Slip stiffness	0.1078	0.4709
Max Long Frc	0.9063	0.6959
Dynamics Vert Stiff (N/mm)	0.8797	0.6999
Fx Peak to Peak	0.8176	0.6385
Fz Peak to Peak	0.2607	0.0336
Avg Long.Frc@Low freq	0.5944	0.0688
Avg Lat.Frc@Mid freq	0.0225	0.3196
Avg Vert.Frc@Mid freq	0.4253	0.5309
Avg Vert.Frc due to Air cavity	0.3127	0.6544

Reference Characteristics

FTC Values	
Rolling Resistance Coeff	4.5400
Cornering Stiff (N/deg)	2496
Max.Lateral Frc	1.0130
Relaxation Length(m)	1.0823
G-function	0.2315
Slip stiffness	3.2140e+03
Max Long Frc	1.1186
Dynamics Vert Stiff (N/mm)	308
Fx Peak to Peak	5072
Fz Peak to Peak	4023
Avg Long.Frc@Low freq	14.8900
Avg Lat.Frc@Mid freq	1.7300
Avg Vert.Frc@Mid freq	1.6467
Avg Vert.Frc due to Air cavity	8.9900

To configure F tire model



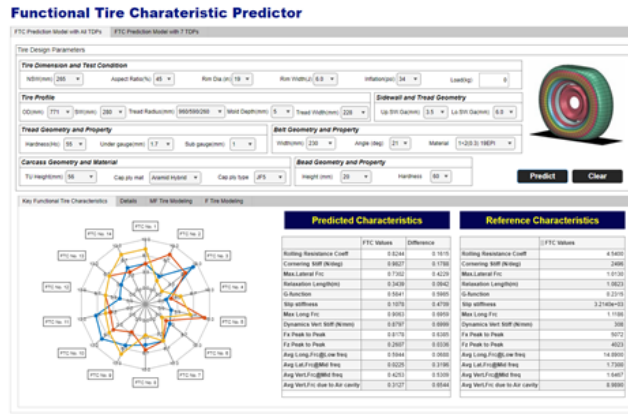
Detail Tire Performance Values

FE, Braking, Road Load		Handling		Ride		NVH	
FTC Values	FTC Values	FTC Values	FTC Values	FTC Values	FTC Values	FTC Values	FTC Values
Rolling Resistance Coeff	4.5400	Rolling Resistance Coeff	4.5400	Rolling Resistance Coeff	4.5400	Rolling Resistance Coeff	4.5400
Cornering Stiff (N/deg)	2496	Cornering Stiff (N/deg)	2496	Cornering Stiff (N/deg)	2496	Cornering Stiff (N/deg)	2496
Max.Lateral Frc	1.0130	Max.Lateral Frc	1.0130	Max.Lateral Frc	1.0130	Max.Lateral Frc	1.0130
Relaxation Length(m)	1.0823	Relaxation Length(m)	1.0823	Relaxation Length(m)	1.0823	Relaxation Length(m)	1.0823
G-function	0.2315	G-function	0.2315	G-function	0.2315	G-function	0.2315
Slip stiffness	3.2140e+03	Slip stiffness	3.2140e+03	Slip stiffness	3.2140e+03	Slip stiffness	3.2140e+03
Max Long Frc	1.1186	Max Long Frc	1.1186	Max Long Frc	1.1186	Max Long Frc	1.1186
Dynamics Vert Stiff (N/mm)	308	Dynamics Vert Stiff (N/mm)	308	Dynamics Vert Stiff (N/mm)	308	Dynamics Vert Stiff (N/mm)	308
Fx Peak to Peak	5072	Fx Peak to Peak	5072	Fx Peak to Peak	5072	Fx Peak to Peak	5072
Fz Peak to Peak	4023	Fz Peak to Peak	4023	Fz Peak to Peak	4023	Fz Peak to Peak	4023
Avg Long.Frc@Low freq	14.8900	Avg Long.Frc@Low freq	14.8900	Avg Long.Frc@Low freq	14.8900	Avg Long.Frc@Low freq	14.8900
Avg Lat.Frc@Mid freq	1.7300	Avg Lat.Frc@Mid freq	1.7300	Avg Lat.Frc@Mid freq	1.7300	Avg Lat.Frc@Mid freq	1.7300
Avg Vert.Frc@Mid freq	1.6467	Avg Vert.Frc@Mid freq	1.6467	Avg Vert.Frc@Mid freq	1.6467	Avg Vert.Frc@Mid freq	1.6467
Avg Vert.Frc due to Air cavity	8.9900	Avg Vert.Frc due to Air cavity	8.9900	Avg Vert.Frc due to Air cavity	8.9900	Avg Vert.Frc due to Air cavity	8.9900



Environment of Model Development

Its Back-end using Optimization Toolbox, Curve fitting Toolbox and so on



MATLAB **App-designer User Interface**

Tire Design variables



Prediction Model (GPR ML)

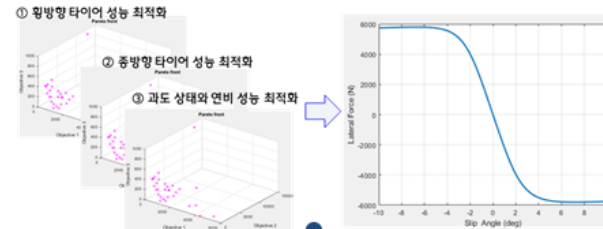
on the way to improve accuracy Of machine learning GPR model with much more FEM tire simulations (by Hankook Tire)

Tire Performance Values

Tire Performance Values



Optimization function



MF Tire Model Parameters



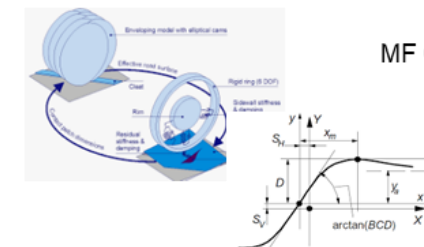
Function to create F tire model



Function To create MF Tire model



F 타이어 모델

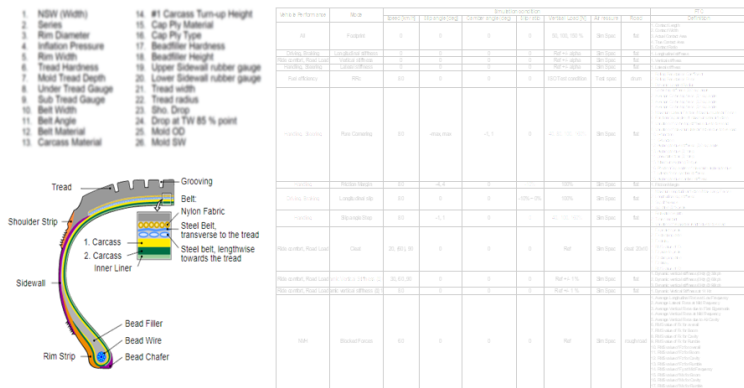


MF 6.2 타이어 모델

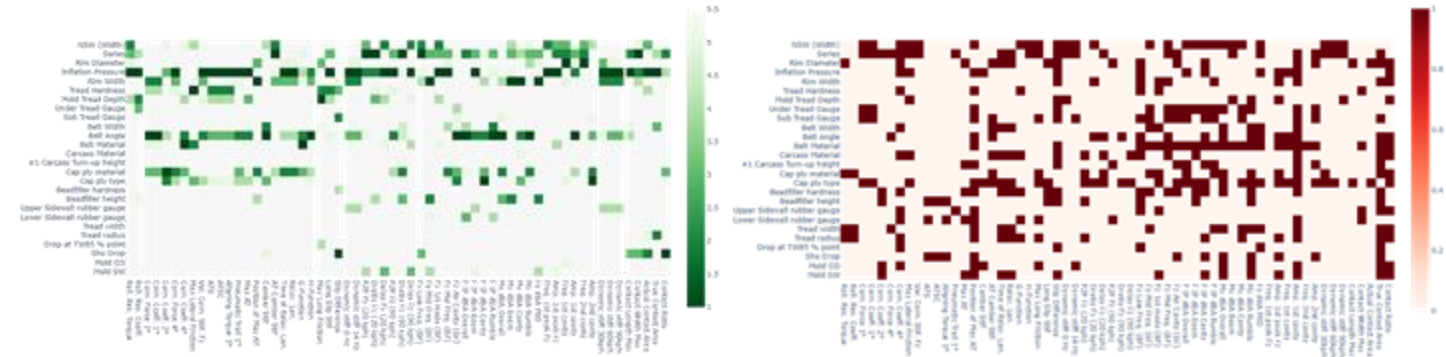
Environment of Model Development

How to create prediction model for FTC (Functional Tire Characteristics)

Tire Design Variables(26)/Simulation Conditions



Sensitivity Analysis to select effective tire design parameters

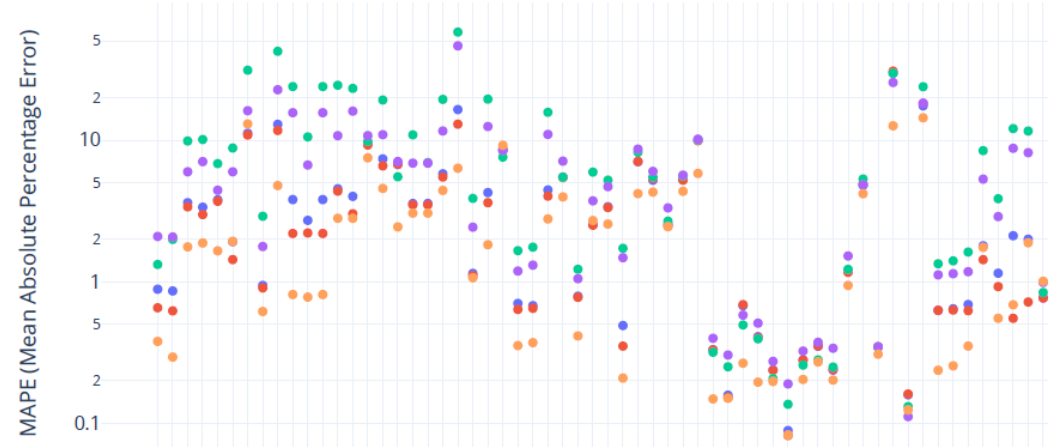


- RidgeMean
- LarsMean
- SVRMean
- KNeighborsRegressorMean
- GaussianProcessRegressorMean

Machine learning algorithm selection using MAPE as evaluation index

Candidates

1. Ridge Regression
2. Least-Angle Regression
3. Support Vector Regression
4. K-nearest Neighbors Regression
5. Gaussian Process Regression



Model V&V Process

VERIFICATION



유효성 검토 (Physical Plausible Check)

Is the model properly configured according to the vehicle specifications/design specifications?
Is it normally simulated in straight/brake/drive/steering/reverse/stop conditions?

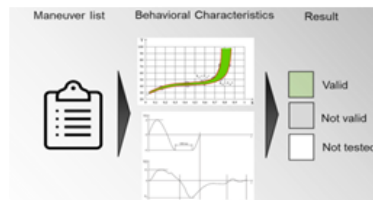
MODEL CHECK



시스템 모델 적합성 검토 (System Model Feasibility)

- 공력 (Aero) - Drag, Lift, Side 공기 저항력
- 파워트레인 (PT) - 엔진 토크, 터보 차저, 변속 패턴(Shift/Lock up)
- 제동 (Brake) - 페달 위치, 제동 토크, 제동 압력, 마스터 실린더 압력
- 타이어 (Tire) - 타이어 F&M (Fx, Fy, Mx, My, Mz)
- 현가 힘요소 (Susp. Force) - 외력(Fspirng, Fdamp, Fstab, Fbps/rbs)
- 현가 K&C (Susp. K&C) - Toe, Camber, Caster, Wheelbase, Tread 변화량

VALIDATION



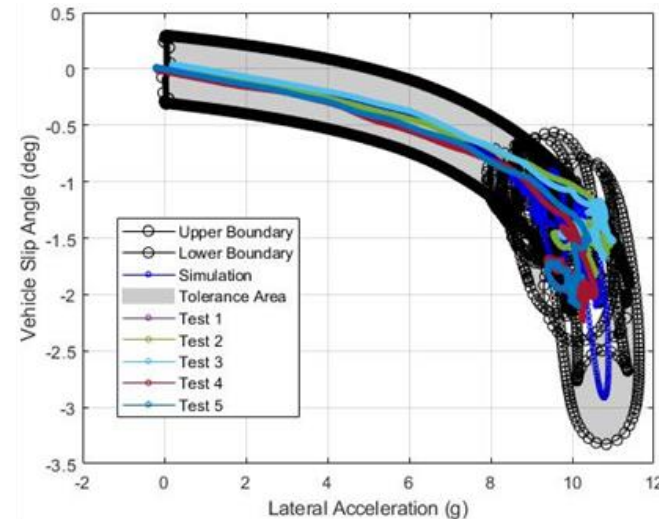
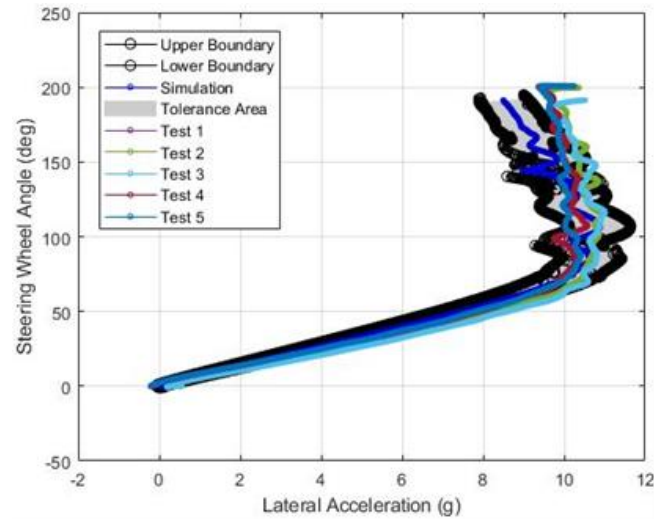
1. 해석 vs 계측간 정합성 검토 (VP Quality)

- Transient, Steady state, Acc/Braking, Coastdown (13 maneuvers)
- ISO4138, ISO22140/7401, ISO19364, ISO 19365

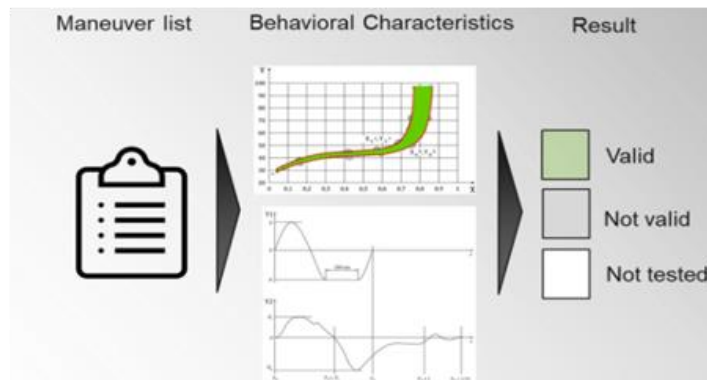
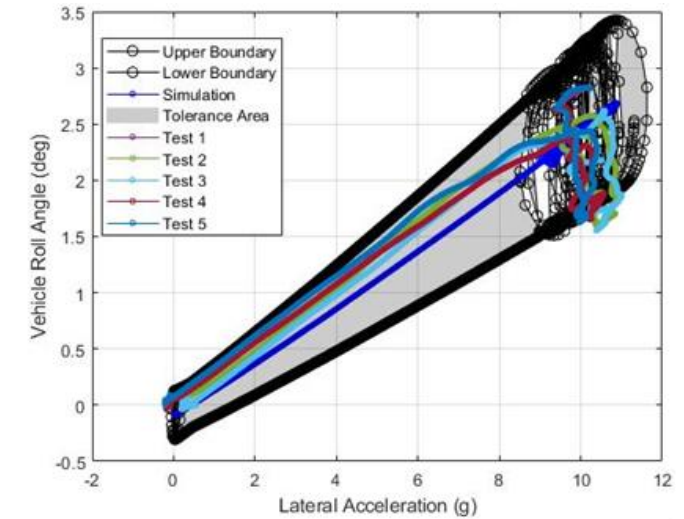
2. 해석 vs 해석(MBD) 정합성 검토 (VP Quality)

- Longitudinal / Lateral Behavior

Model V&V Process



[ISO 19364 시험 : Counter Clockwise]



$$X_T = X - \Delta Y \epsilon_X^2 / D \quad X_B = X + \Delta Y \epsilon_X^2 / D$$

$$Y_T = Y + \Delta X \epsilon_Y^2 / D \quad Y_B = Y - \Delta X \epsilon_Y^2 / D$$

Table 1 — Offsets and gains used to define tolerances ϵ_X and ϵ_Y for constant-radius tests

Variable on Y-axis	X offset (m/s ²)	X gain	Y offset (deg)	Y gain
Steering wheel angle (deg)	0,1	0,06	1,0	0,03
Sideslip angle (deg)	0,1	0,06	0,3	0,04
Roll angle (deg)	0,1	0,06	0,2	0,2

Summary

- The demand for vehicle/system model for SW virtual verification/validation(V&V) and calibration is significantly/remarkably increased for SW development efficiency.
- MATLAB/Simulink is widely used in HMC vehicle dynamics modeling process thanks to useful and powerful toolbox and MATLAB/Simulink is very open/efficient tool to connect the different models and to operate different tool chain.
- Hyundai is on the way to develop Simulink based vehicle dynamics model including PT/PE systems in Powertrain Blockset to easily integrate control models.
- Current vehicle model quality (fidelity of system model) and qualification process need to be improved for SW virtual calibration at high long./lat. acc range. But vehicle models are widely used across many application areas for function validating, fail safe, fault diagnosis, regulation certification, virtual calibration (at low~mid acc range)
- Objective model validation index is under investigation and its criteria will be quantified in order for consistency of model quality especially for SW virtual calibration in terms of vehicle behaviors

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Thank you

